

Reliability evaluation on weighted graph metrics of fNIRS brain networks

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Background: Resting-state fNIRS (R-fNIRS) imaging data has proven to be a valuable technique to quantitatively characterize functional architectures of human brain network. However, whether the brain network metrics derived using weighted brain network model is test-retest (TRT) reliable remains largely unknown.

Methods: Here, we firstly constructed weighted brain networks on a group of 18 participants, and then applied graph-theory approach to quantify topological parameters of each weighted network. The intraclass correlation coefficient (ICC) was further applied to quantify the TRT reliability of network metrics.

Results: We found that the reliability of the weighted network metrics is threshold-sensitive, and most of these network metrics showed fair to excellent reliability. Specifically, the global network metrics, e.g., clustering coefficient, path length, local efficiency and global efficiency were of excellent level reliability (ICC >0.75) on both HbO and HbR signals. The nodal network metrics, e.g., degree and efficiency, generally also showed excellent level reliability on both HbO and HbR signals, and the reliability of these two metrics was better than that of nodal betweenness.

Conclusions: Overall, these findings demonstrated that most weighted network metrics derived from fNIRS are TRT reliable and can be used for brain network research.

Keywords: Functional connectivity; weighted network; graph theory; small-world; module

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Introduction

The application of graph theory to brain networks has proved great potential in investigating network organizations of the human brain (1,2). A variety of neuroimaging and neurophysiological techniques (e.g., structural MRI, diffusion MRI, functional MRI and electroencephalography/magnetoencephalography) have consistently observed the brain to be organized into a "small-world" and modular network structure, making it efficient in local information processing and global information integration (3-5).

Functional near-infrared spectroscopy (fNIRS) is an

emerging neuroimaging technology with a lot of advantages, e.g., low cost, high portability, large motion robustness and friendly ecological validity. With whole-brain fNIRS imaging data, many studies have demonstrated that the intrinsic characteristics of human brain networks, such as small-world efficiency, modularity and highly connected hubs, can also be revealed by resting fNIRS imaging data. The reliability of graphic metrics of fNIRS brain networks were acceptable, e.g., with fair to excellent reliability level, which makes fNIRS imaging-based technique be convincingly applied to the developmental and clinical neuroscience studies (6-8). The evaluation of stability and

reproducibility of fNIRS brain network showed that the duration of the fNIRS signal scanning is related to stable and reproducible functional brain network features, e.g., stable, reproducible and reliable brain functional connectivity and topological network properties can be obtained after 1 and 5 min of fNIRS signal acquisition, respectively (9,10). These methodological researches provide fundamental evidences to support the feasibility and reliability as using fNIRS imaging technique for human brain network studies. Furthermore, for the application study, researchers also revealed that fNIRS imaging data can characterize brain network changes during development from children to adults (11). For instance, Cai et al. pointed out that the properties of smallworldness and modularity were not significantly different across development, but global and local efficiency showed important developmental changes over development (11). Recently, Li et al. showed that the children with autism spectrum disorders (ASD) had decreased network efficiency compared to healthy controls, and the ASD children with a relatively higher level of autistic behaviors showed much lower network efficiency (12). These accumulated researches suggest that the emerging fNIRS imaging technique has a great potential to be used to explore development and changes of the human brain network in future research.

However, it needs to point out that the current brain network studies were mainly based on binary networks and constructed graphic network by setting each edge as 0 (under the threshold) or 1 (above the threshold). As such, the binary network is of relatively simple calculation and easy to understand. However, compared to binary network, the weighted network (as another important network model), was constructed by calculating magnitudes of correlational or causal interactions between time series (2). The weighted network has better performance in filtering the influence of weak and potentially non-significant links (13). But it remains largely unknown whether the weighted network metrics derived from fNIRS imaging data are TRT reliable or not.

Thus, in this study, we conducted a comprehensive assessment of the TRT reliability of weighted network metrics of fNIRS brain networks. The data was a group of healthy young adults over two sessions with a 20-minute interval between sessions. For each participant, we constructed a weighted functional networks by computing temporal correlations between the time series of pairs of channels. We further analyzed global network metrics and regional nodal metrics using graph-theoretical approaches. Finally, intraclass correlation coefficients (ICC) were calculated to assess the TRT reliability of these network metrics. The human brain weighted network where each connection above the threshold is unique and retains its primary feature.

Methods

Subject and protocol

The data was same to our previous study of reliability evaluation of binary network (6). Twenty-one healthy righthanded subjects aged 21-27 years old (17 male, average age: 24.5) were recruited in this study. All subjects were undergraduate students that came from Beijing Normal University. This study was supported by the Review Board at the State Key Laboratory of Cognitive Neuroscience and Learning, Beijing Normal University, and informed consent form was acquired from each participate ahead of the experiment. All participants can quit the test at any time if they felt uncomfortable. Two eleven-minute of resting-state fNIRS scanning were carried out on all participates. The scanning duration was ~20 minutes. During fNIRS data acquisition, each subject was instructed to sit in the chair quietly and keep his/her eyes closed without falling asleep and movements.

Data acquisition and preprocessing

A continuous wave (CW) near infrared optical imaging system (CW6, TechEn Inc., MA, USA) was adopted to collect the fNIRS data. There were 12 laser sources and 24 detectors in this system that constituted 46 different measurement channels to cover almost the whole head, including the frontal, temporal, parietal and occipital lobes. The source-detector distance was 3.2 cm. The arrangement of the probes was based on the international 10-20 system of electrode placement with the external auditory canals and vertex of each participant as placemark, and the positions were measured at both scanning sessions to confirm accordance location. Figure 1 showed the schematic diagram of the probe array layout. Of note, the instrument generated two wavelengths of near-infrared light (690 and 830 nm) and measured time courses of concentration changes in both oxyhemoglobin (HbO) and deoxyhemoglobin (HbR) for all measurement channels. The sampling rate for the optical signal was set to 25 Hz.



Figure 1 The arrangement of fNIRS measurement channels. (A) Spatial distribution of the whole-head 46 measurement channels on a brain template; (B) the schematic of 12 sources and 24 detectors between which there are all 46 channels.

Data processing

Ten-minute stable signal was extracted from raw hemodynamic time course for each participant. Similar to our previous studies (6,14), band-pass filtering with cutoff frequencies of 0.009 and 0.08 Hz was used to extract neural activity signal and meantime to reduce the effects of nonneural signals (e.g., respiratory and cardiac noises) (15-17). We further adopted independent component analysis (ICA) to reduce the influence of head motion and superficial noise in neuronal activity signal. The detailed information can be found in the series resting-state fNIRS studies (6,18,19) in our groups. Three subjects were excluded due to poor contact between the probe and scalp, leaving 18 subjects in this study for the further network analysis.

Weighted network construction

Nodes and edges are two basic elements of a weighted network. In fNIRS study, the nodes were defined as measurement channels and edges were defined as functional connectivity between nodes. In weighted network, functional connectivity was quantified by computing Pearson correlation coefficients for the time series between pairs of nodes. This procedure generated a 46×46 correlation matrix for each subject. The correlation matrix was thresholded at sparsity ranging from 0.01–0.5 at an interval of 0.01 to obtain a series of weighted networks. For each weighted network, the weights of the edges were equal to the absolute connectivity strengths, and the smaller than the designed thresholds were set to 0 (*Figure 2*).

Weighted network analysis

Global network metrics and regional nodal metrics were calculated for each thresholded weighted network, respectively. The global network metrics characterized global topological characteristics of the whole-brain network and the regional nodal network metrics descripted regional properties of the whole-brain network. The global network metrics included small-world properties (clustering coefficient, C_p , characteristic path length, L_p , normalized clustering coefficient, γ , and normalized characteristic path length, λ and small-world index, σ), efficiency parameters (global efficiency, E_{glob} , and local efficiency, E_{loc}), hierarchy (β) and modularity (Q). The regional nodal network metrics included nodal degree (K_{nod}), nodal efficiency (E_{nod}) and nodal betweenness (N_{bc}).

Test-retest (TRT) reliability evaluation

We used ICC to assess the TRT reliability of the global and local metrics of weighted brain networks (20). The ICC was calculated according to the following equation:

$$ICC = \frac{MS_b - MS_w}{MS_b + (k-1)MS_w}$$

where MS_b is between-subject variance, MS_w is within-



Figure 2 Flow chart of the test-retest reliability analysis.

subject variance and k is the number of the repeated measurements (20). For each measure of the weighted network, the ICC value was calculated directly according to quantitative values of 18 pairs of network metrics across session 1 and session 2. Area under the curve (AUC) of the sparsity: 0.1–0.5 (interval =0.01) were used as measurements to evaluate ICCs of global and local metrics. All reliability indices investigated above were evaluated according to the criteria that ICC value from 0 to 0.25 indicates poor reliability; 0.25 to 0.4 indicates low reliability, 0.4 to 0.6 indicates fair reliability; 0.6 to 0.75 indicates good reliability and 0.75 to 0.1 indicates excellent reliability (21,22). Obviously, for any metric, if the between-subject variance is larger than the withinsubject variance, the ICC values will be negative. This kind of situation is impossible in theory (23), and the reason for negative values is still unclear (24). So, we set the negative values to zero as generally suggested (18,19).



Figure 3 TRT reliability of global network metrics as a function of sparsity threshold. The first and the second rows represent the ICC for HbO and HbR, respectively. Almost all metrics exhibited high reliability through most of the thresholds. Five colors correspond to five different reliability grades. The red, yellow, green, cyan, and blue colors represent excellent (0.75 < ICC < 1), good (0.6 < ICC < 0.75), fair (0.4 < ICC < 0.6), low (0.25 < ICC < 0.4), and poor (ICC < 0.25) reliability.

Results

TRT reliability of global network metrics

In the present study, individual networks were constructed at the same sparsity level by applying subject-specific correlation thresholds to individual correlation matrices. Sparsity threshold ensures all resultant networks to have comparable topological structures of the same number of edges. *Figure 3* showed the TRT reliability of these nine global network metrics over the sparsity range of 0.01 to 0.5 with 0.01 as interval. Generally, most global network metrics exhibited fair to excellent reliability, irrespective of the ICC calculated from HbO or HbR signals. For example, the clustering coefficient, characteristics path length, global efficiency and local efficiency showed excellent reliability level across wide threshold range. Meanwhile, it was also noticed that the reliability of the network metrics displayed obvious differences even if at the same sparsity thresholds.

Furthermore, we calculated the AUC of each network measure to test significant differences in each metric across subjects between sessions. The results were shown in *Table 1*. These nine global network measures have not shown significantly different (paired *t*-tests, P>0.05, *Table 1*), suggesting a high similarity for global network measures

 Table 1 Significant differences in the global network metric (AUC)

 between sessions revealed by a paired *t*-test

Global metrics	t	Р
HbO		
C _p	-0.83	0.42
$L_{ ho}$	-0.23	0.82
γ	1.59	0.13
λ	0.06	0.95
σ	1.64	0.12
E _{loc}	-0.33	0.75
E_{glob}	0.10	0.92
Q	1.52	0.15
β	0.98	0.34
HbR		
$C_{ ho}$	-0.63	0.54
L _p	0.37	0.72
γ	-1.08	0.29
λ	0.01	0.99
σ	-1.02	0.32
E _{loc}	-1.03	0.32
E _{glob}	-1.04	0.31
Q	-0.69	0.50
β	-0.85	0.41

between sessions at the individual level. We also used the AUC of each metric to calculate the reliability index (*Figure 4*). For both HbO and HbR signals, all network metrics consistently exhibited fair to excellent reliability.

TRT reliability of nodal metrics

The nodal reliability of degree, efficiency and betweenness were shown in *Figure 5*. These measures varied depending on the sparsity threshold values. Obviously, the ICC values of nodal degree and nodal efficiency exhibited very similar patterns and the reliability was better than that of nodal betweenness for both HbO and HbR signal. It was also found that almost all nodes exhibited fair to excellent reliability at most sparsity threshold values (e.g., from 0.01 to 0.5). Specifically, for nodal degree and nodal efficiency, the metric reliability was similar to each other for both



Figure 4 Threshold-independent reliability analysis of global network metrics. The area under the curves (AUCs) of nine global network metrics: C_p , L_p , γ , λ , σ , E_{loc} , E_{glob} , Q, β for HbO and HbR, respectively. HbO signals showed better performance than HbR signals on the threshold-independent scale.

HbO and HbR signals, and the reliability also exhibited better performance than that from nodal betweenness. Figure 6 shows the distribution of nodal metric reliability over total 46 channels on the brain schematic diagram using AUC as a measurement. For both HbO and HbR, most of these nodes showed fair to excellent reliability on nodal degree and nodal efficiency. The reliability of nodal betweenness was relatively much poorer or lower at most nodes compared to that in nodal degree and efficiency. We further used a two-factor repeated measures ANOVA to evaluate the influence of different nodal metrics (degree, efficiency and betweenness) and different signals (HbO, HbR) on nodal reliability. Threshold-independent measure AUC was used to carry out the statistical analysis. The results demonstrated a significant main effect of nodal metrics [F (2, 90)=218.66, P<0.0001] (Figure 7). And there was also not significant interaction between the nodal metrics and different concentration signals. These findings suggested that HbO and HbR signals possibly have similar performance on weighted network properties. The results

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Figure 5 TRT reliability of nodal centrality metrics as a function of sparsity threshold. The nodal metric reliability was derived from HbO and HbR, respectively. The degree and efficiency exhibited fair to excellent reliability at most thresholds but betweenness showed poor reliability at most thresholds.

of post hoc pairwise comparisons indicated that reliability of nodal betweenness was significantly lower than nodal degree and nodal efficiency both for HbO and HbR signals (P<0.0001).

Discussion

Previous study had verified the feasibility and reliability of combining resting-state fNIRS and graph theory to assess the topological organization of binary brain network (14). In this study, we specifically evaluate the TRT reliability of weighted fNIRS brain network. We constructed weighted networks at several thresholds ranging from 0.01 to 0.5 (interval =0.01). Based on the constructed network, we calculated nine global network metrics including small-worldness, global and local efficiency, modularity and hierarchy and three nodal metrics including nodal degree, nodal efficiency and nodal betweenness. Then we evaluated the reliability of these metrics using the threshold-independent index AUC to show the reliability of each metric.

Previous studies showed that most of these global network metrics and two of these nodal metrics (i.e., nodal degree and nodal efficiency) exhibited great reliability at a number of thresholds. For those studies, the authors

mainly used binary networks rather than weighted networks to evaluate the TRT reliability of graph metrics. The weighted graph metrics was more and more popular in recent brain organization network researches. The weights in anatomical networks may represent the size, density, or coherence of anatomical tracts, and in functional and effective networks it may represent respective magnitudes of correlational or causal interactions which can not be neglected (2). And weighted networks usually focuses on somewhat different and complementary aspects of network organization and may be especially useful in filtering the influence of weak and potentially non-significant links (13). However, for fNIRS study, there remains largely unknown how the TRT reliability of topological organization of weighted network. In this study, we found that almost all global metrics exhibited fair to excellent reliability at most sparsity thresholds ranging from 0.01 to 0.5 except λ for HbO data and λ , σ , Q and β showed very poor reliability at low thresholds (sparsity <0.1) for HbR data. The explanation of poor ICC value for HbR data is that the metric λ (normalized characterized path length: index for small-worldness) may not have practical meaning in weighted network. Latora, Marchiori (25) had proposed global efficiency and local efficiency in weighted network as replacement of characteristic path length and

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Poor Low Fair Good Excellent

Figure 6 Threshold-independent reliability of nodal metrics. The area under the curves (AUCs) were shown in the spatial brain. Degree and efficiency showed better reliability than betweenness.

clustering coefficient respectively in binary network because characteristic path length and clustering coefficient were used to examine small-worldness based on the hypothesis that the generic graph G is assumed to be unweighted, simple, sparse and connected (26). And for HbR data, we can infer that the sparsity threshold was too low to contain enough significant edges (neglect of lots of meaningful connection) so that several global metrics showed poor reliability. Then we used the threshold-independent index AUC to present the reliability. We found that for HbO data, except for λ , all global metrics exhibited fair to excellent reliability as expected, but for HbR data, the ICC values demonstrated very unbalanced distribution of which λ , σ , and Q exhibited bad reliability but others exhibited relatively good reliability. Notably, C_{p} , L_{p} and E_{loc} , E_{glob} demonstrated very similar reliability pattern which

is consistent with the initial proposed theory of smallworldness in weighted network (25). A paired *t*-test showed the similarity of nine global network metrics both for HbO and HbR signals. And we also calculated the reliability of nodal network metrics from which we can see that almost all nodes exhibited fair to excellent reliability for nodal degree and nodal efficiency at nearly all sparsity thresholds ranging from 0.01 to 0.5 (interval =0.01). On the contrary, nodal betweenness exhibited poor reliability at most thresholds. In order to numerically evaluate the reliability of nodal reliability, we calculated the AUC of all sparsity thresholds. The results showed very similar ICC values to the conclusion from the reliability at the whole thresholds that nodal degree and nodal efficiency exhibited relatively great reliability and on the contrary nodal betweenness had poor reliability. We can also see from the whole figure that

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Figure 7 The results of two-way repeated ANOVA. There was no significant difference between the reliability of HbO and HbR signals. But for the two signals, there were significant differences between degree, efficiency and betweenness. ***, the P value<0.001 of the two-way repeated ANOVA.

the results from the HbR signal exhibited higher reliability compared to HbO signal. And the statistical analysis also proved that betweenness was not an effective measurement for discussing brain network organization.

In addition, our results of weighted network also showed relatively high network metrics reliability in most network metrics, such as C_{ν} and L_{ν} , for both HbO and HbR signals. These findings were also consistent with our previous investigation of network metric reliability from binary network (27). Furthermore, we also found that there were differences in the network metric reliability between weighted network and binary network. For example, the λ in the weighted network performed relatively worse performance in HbO signal, whereas that exhibited relatively high reliability (i.e., excellent level) in the binary network for two hemoglobin concentration signals. Indeed, weighted networks could characterize network topology more precisely and detect more subtle network topological changes than binary networks due to the consideration of connectivity strength (25,28,29). However, this is not necessary to mean better reliability for weighted networks since the possibility that weighted networks may introduce simultaneously extra noise or overly model individual specific details. All these may lead to more within-subject variance (i.e., variance across scans) and thus lower reliability. This suggests that the observed reliability derived from actual R-fNIRS data were affected by various factors, not a single factor of numerical changes in functional

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connectivity.

Our findings confirmed the TRT reliability of combining fNIRS and graph theory to evaluate the topological organization of weighted brain. We also demonstrated that most global and local network metrics exhibited good reliability especially for small-worldness and efficiency in a weighted network which can be very beneficial to further studies.

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Footnote

Conflicts of Interest: The authors have no conflicts of interest to declare.

Ethical Statement: This study was supported by the Review Board at the State Key Laboratory of Cognitive Neuroscience and Learning, Beijing Normal University, and informed consent form was acquired from each participate ahead of the experiment.

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