

A chain reaction approach to modelling gene pathways

Gary C. Cheng^{1*}, Dung-Tsa Chen^{2*}, James J. Chen³, Seng-jaw Soong⁴, Coral Lamartiniere⁵, Stephen Barnes⁶

¹Department of Mechanical Engineering, University of Alabama at Birmingham, HOEN 320A, 1530 3rd Ave. S., Birmingham, AL 35294-4461, USA;

²Department of Biostatistics, Moffitt Cancer Center, 12902 Magnolia Drive, Tampa, FL 33612, USA; ³Division of Biometry and Risk Assessment, National Center for Toxicological Research, Food and Drug Administration, Jefferson, AR 72079, USA; ⁴Biostatistics and Bioinformatics Unit, Comprehensive Cancer Center, University of Alabama at Birmingham, 153 Wallace Tumour Institute, 1824 6th Avenue South, Birmingham, AL 35294, USA; ⁵Department of Pharmacology and Toxicology, University of Alabama at Birmingham, VH 124, 1670 University Boulevard, Birmingham, AL 35294, USA; ⁶Department of Pharmacology and Toxicology, University of Alabama at Birmingham, MCLM 452, 1918 University Boulevard, Birmingham, AL 35294, USA

*These authors contributed equally to this work

Contributions: (I) Conception and design: GC Cheng, DT Chen, JJ Chen; (II) Administrative support: None; (III) Provision of study materials or patients: SJ Soong; (IV) Collection and assembly of data: C Lamartiniere, S Barnes; (V) Data analysis and interpretation: GC Cheng, DT Chen, JJ Chen; (VI) Manuscript writing: All authors; (VII) Final approval of manuscript: All authors.

Corresponding to: Dung-Tsa Chen. Department of Biostatistics, Moffitt Cancer Center, 12902 Magnolia Drive, Tampa, FL 33612, USA.
Email: dung-tsa.chen@moffitt.org.

Background: Of great interest in cancer prevention is how nutrient components affect gene pathways associated with the physiological events of puberty. Nutrient-gene interactions may cause changes in breast or prostate cells and, therefore, may result in cancer risk later in life. Analysis of gene pathways can lead to insights about nutrient-gene interactions and the development of more effective prevention approaches to reduce cancer risk. To date, researchers have relied heavily upon experimental assays (such as microarray analysis, etc.) to identify genes and their associated pathways that are affected by nutrient and diets. However, the vast number of genes and combinations of gene pathways, coupled with the expense of the experimental analyses, has delayed the progress of gene-pathway research. The development of an analytical approach based on available test data could greatly benefit the evaluation of gene pathways, and thus advance the study of nutrient-gene interactions in cancer prevention. In the present study, we have proposed a chain reaction model to simulate gene pathways, in which the gene expression changes through the pathway are represented by the species undergoing a set of chemical reactions. We have also developed a numerical tool to solve for the species changes due to the chain reactions over time. Through this approach we can examine the impact of nutrient-containing diets on the gene pathway; moreover, transformation of genes over time with a nutrient treatment can be observed numerically, which is very difficult to achieve experimentally. We apply this approach to microarray analysis data from an experiment which involved the effects of three polyphenols (nutrient treatments), epigallo-catechin-3-O-gallate (EGCG), genistein, and resveratrol, in a study of nutrient-gene interaction in the estrogen synthesis pathway during puberty.

Results: In this preliminary study, the estrogen synthesis pathway was simulated by a chain reaction model. By applying it to microarray data, the chain reaction model computed a set of reaction rates to examine the effects of three polyphenols (EGCG, genistein, and resveratrol) on gene expression in this pathway during puberty. We first performed statistical analysis to test the time factor on the estrogen synthesis pathway. Global tests were used to evaluate an overall gene expression change during puberty for each experimental group. Then, a chain reaction model was employed to simulate the estrogen synthesis pathway. Specifically, the model computed the reaction rates in a set of ordinary differential equations to describe interactions between genes in the pathway (A reaction rate K of A to B represents gene A will induce gene B per unit at a rate of K ; we give details in the “method” section). Since disparate changes of gene expression may cause numerical error problems in solving these differential equations, we used an implicit scheme to address

this issue. We first applied the chain reaction model to obtain the reaction rates for the control group. A sensitivity study was conducted to evaluate how well the model fits to the control group data at Day 50. Results showed a small bias and mean square error. These observations indicated the model is robust to low random noises and has a good fit for the control group. Then the chain reaction model derived from the control group data was used to predict gene expression at Day 50 for the three polyphenol groups. If these nutrients affect the estrogen synthesis pathways during puberty, we expect discrepancy between observed and expected expressions. Results indicated some genes had large differences in the EGCG (e.g., Hsd3b and Sts) and the resveratrol (e.g., Hsd3b and Hrmt12) groups.

Conclusions: In the present study, we have presented (I) experimental studies of the effect of nutrient diets on the gene expression changes in a selected estrogen synthesis pathway. This experiment is valuable because it allows us to examine how the nutrient-containing diets regulate gene expression in the estrogen synthesis pathway during puberty; (II) global tests to assess an overall association of this particular pathway with time factor by utilizing generalized linear models to analyze microarray data; and (III) a chain reaction model to simulate the pathway. This is a novel application because we are able to translate the gene pathway into the chemical reactions in which each reaction channel describes gene-gene relationship in the pathway. In the chain reaction model, the implicit scheme is employed to efficiently solve the differential equations. Data analysis results show the proposed model is capable of predicting gene expression changes and demonstrating the effect of nutrient-containing diets on gene expression changes in the pathway.

One of the objectives of this study is to explore and develop a numerical approach for simulating the gene expression change so that it can be applied and calibrated when the data of more time slices are available, and thus can be used to interpolate the expression change at a desired time point without conducting expensive experiments for a large amount of time points. Hence, we are not claiming this is either essential or the most efficient way for simulating this problem, rather a mathematical/numerical approach that can model the expression change of a large set of genes of a complex pathway. In addition, we understand the limitation of this experiment and realize that it is still far from being a complete model of predicting nutrient-gene interactions. The reason is that in the present model, the reaction rates were estimated based on available data at two time points; hence, the gene expression change is dependent upon the reaction rates and a linear function of the gene expressions. More data sets containing gene expression at various time slices are needed in order to improve the present model so that a non-linear variation of gene expression changes at different time can be predicted.

Key Words: Chain reaction; gene expression change; estrogen synthesis pathway; nutrient diets



Submitted Apr 15, 2012. Accepted for publication May 11, 2012.

DOI: 10.3978/j.issn.2218-676X.2012.05.06

Scan to your mobile device or view this article at: <http://tcr.thepbpc.org/article/view/387/757>

Background

Cancer can be viewed as a chronic disease that may be influenced by genetic and nutritional factors at various stages in its natural history. The interaction of genes and nutrient components is associated with cancer incidence and tumor behaviour (1-3). It is estimated that one third of all cancer cases may be influenced by diet and associated lifestyle factors, such as food and excess calories for increasing cancer risk (4). On the other hand, many dietary components may have anti-cancer effects by affecting simultaneously multiple cancer processes, such as

carcinogen metabolism, hormonal balance, cell signalling, cell-cycle control, and angiogenesis (5). Polyphenols are a group of dietary components found in plants, characterized by the presence of more than one phenol group per molecule. It has been suggested that polyphenols are antioxidants with potential health benefits in reduction of cancer risk (6). Sources of polyphenols include green tea, red wine, soybeans and other fruits and vegetables. To study the interaction of polyphenols on gene expression, the UAB Center for Nutrient-Gene Interaction (CNGI, a NCI funded research program) conducted experiments to examine three dietary polyphenols: genistein from soy,

resveratrol from grapes, and epigallocatechin 3-gallate (EGCG) from green tea. A component of this study is to investigate the nutritional modulation of genetic pathways of estrogen synthesis and metabolism using microarray data.

Various pathway databases and methods (e.g., KEGG, GENMAPP, REACTOME, CYTOSCAPE, and BIOCARTA) are available on the internet for pathway analysis (7-12). These curated databases are useful resources to study biological processes, such as the pathways of intermediary metabolism, regulatory pathways, and signal transduction. They also help investigators gain insight into the potential functions of new genes. Since the databases contain massive amounts of information, it becomes challenging for researchers to convert the enormous amount of information into useful knowledge. Many approaches have been developed to provide parsimonious models to analyze gene pathways. For example, MAPPFinder and Pathway-Miner are bioinformatics tools to create global gene expression profiles across biological pathways (13,14). They classify genes by integrating the gene ontology (GO) annotations based on metabolic, cellular and regulatory pathways. Typically, a top list of genes selected by one of these statistical methods is mapped onto pathways with gene product association networks for genes that occur in the pathways. A z-score or the Fisher exact test is then used to test statistical significance of pathways. The pathways can be ranked in accordance with the P values. These tools depict biological interaction among genes and provide insights to study associations of the biological pathways with research outcomes (e.g., disease versus non-disease or treatment versus control). Though these methods provide valuable statistical assessment of gene expression changes, they do not offer the quantitative description of the dynamic relationship and interaction between the genes of interest. Hence, it is difficult to use these methods to disentangle biological processes, and to predict the outcome of gene expression changes due to different initial gene profiles and treatment processes.

The chain reaction model has been widely used in the engineering field to simulate chemical reactions that occur in combustion devices such as jet and rocket engines, etc. (15,16). The chain reaction model contains a set of chemical reactions, where the rate of each reaction was estimated either based on the molecular collision theory of quantum mechanics or from the test data (such as shock tube experiments). In the present study, we propose a chain reaction model to simulate gene

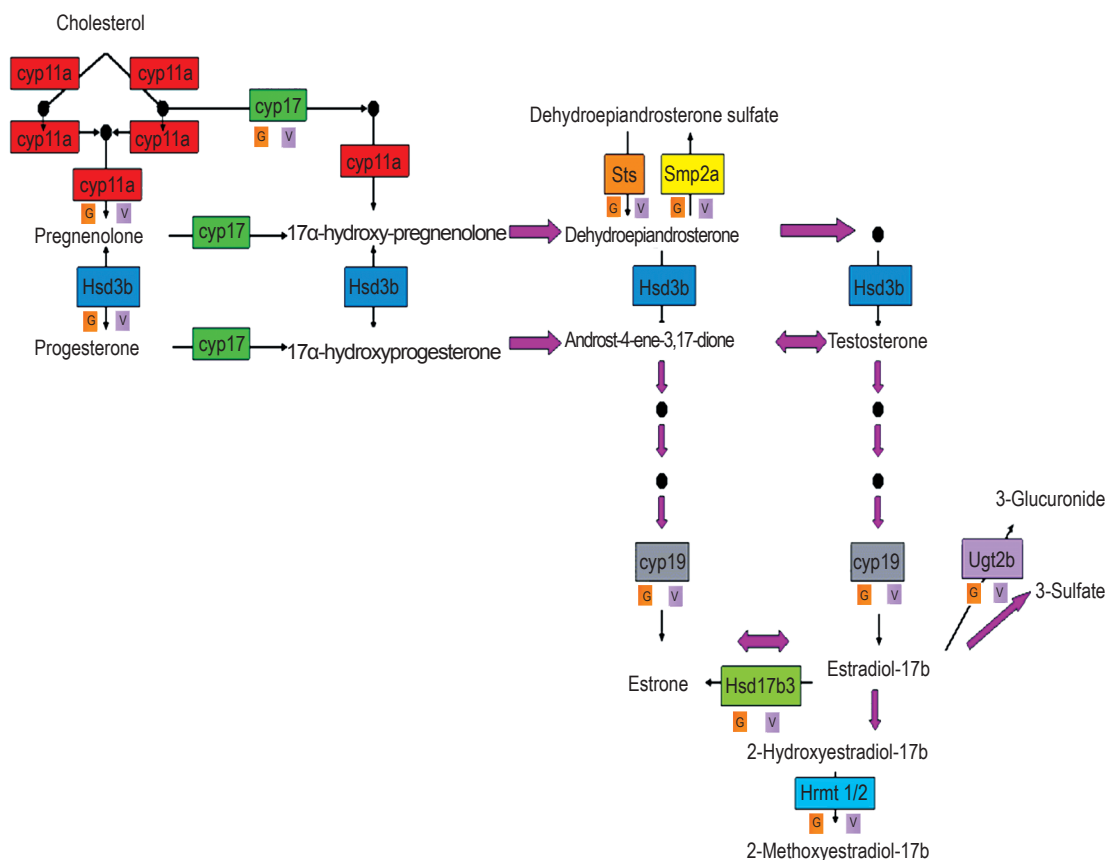
pathways as an alternative. The proposed chain reaction model provides a systematic approach for pathway level analyses such that parametric studies of various pathways, selections of genes and nutrient-gene interaction can be performed in an efficient and cost-effective manner. In the proposed model, we use the regulated genes as a set of reacting species and calculate the species changes as the gene expression changes. This approach is applied to a microarray experiment designed to study the nutrient effects on the estrogen synthesis pathway during puberty in which nutrient-, time-, and gene- interactions play a critical role.

Data example

Estrogen synthesis pathway

Figure 1 shows an estrogen synthesis pathway, developed at the Center for Nutrient-Gene Interaction (CNGI) at the University of Alabama at Birmingham (UAB). Estrogens are formed in a series of metabolic channels starting from cholesterol. For example, Desmolase (CYP11a) removes part of the cholesterol side chain to produce the first steroid pregnenolone. Pregnenolone, in turn, undergoes 17 α -hydroxylation by CYP17. 17 α -hydroxypregnenolone is converted to the adrenal androgen dehydroepiandrosterone (DHEA) by CYP11a. Pregnenolone is also converted to progesterone by 3 β -hydroxysteroid dehydrogenase (HSD3b1). Progesterone is converted to testosterone by CYP17, CYP11a and HSD3b1. Aromatase (CYP19) converts testosterone and androstenedione to 17 β -estradiol and estrone, respectively. Estrone is reversibly converted to estradiol by 17 β -hydroxysteroid dehydrogenase (HSD17b3). Conjugation of estrogens to 3-glucuronides and 3-sulfates is catalyzed by UDP-glucuronosyltransferases (UGTs) and PAPS-sulfotransferases (SULTs), respectively. There are also corresponding hydrolases (glucuronidases and sulfatases) that may selectively release estrogens from conjugates that circulate in the blood.

Polyphenols have been shown to inhibit the enzymatic properties of many enzymes in the estrogen synthesis pathway (17,18). However, it is less known about the effects of the polyphenols on the rates of transcription and translation of the genes encoding these enzymes (19). The use of microarray analysis may provide important information about the regulation of these enzymes and identifying gene and protein partners that modulate their activities.



Experimental design

–80 °C for approximately 6 months. The samples were run on the Affymetrix GeneChip® Rat Genome 230 2.0 (RAE 230) in the UAB Comprehensive Cancer Center Microarray Facility. Data quality was checked using a 2D image plot (20); no problems in these microarrays were found. The Affymetrix gene chip (i.e., RAE 230) contains 31,099 genes and ESTs. Among these genes, there are 8 genes involved in the estrogen synthesis pathway as shown in *Table 1*. We used the data on these 8 gene expressions to analyze the estrogen synthesis pathway.

We first performed a statistical analysis to test the time factor on the estrogen synthesis pathway. Since we have interest in this particular estrogen synthesis pathway (not to compare to a known pathway), we used the self-contained gene set methods to evaluate if this pathway

Table 1 Descriptive statistics of gene expressions in estrogen synthesis pathway at Day 21 and Day 50

Experimental group	Gene name	day 21		day 50	
		Mean	SD	Mean	SD
Control	Cyp11a1	6.28	0.59	5.24	0.36
	Cyp17a1	0.96	0.41	1.4	0.77
	Hsd3b	2.93	0.96	3.52	0.68
	Hsd17b3	3.3	0.99	2.98	0.98
	Hrmt1l2	9.39	0.24	9.38	0.17
	Sts	6.31	0.33	6.34	0.36
	Smp2a	3.1	0.91	2.4	0.94
	Ugt2b	1.95	0.92	1.73	1.11
EGCG	Cyp11a1	6.03	0.31	5.48	0.37
	Cyp17a1	1.27	0.82	1.76	0.88
	Hsd3b	3.47	0.72	3.35	0.56
	Hsd17b3	3.43	1.07	3.6	0.71
	Hrmt1l2	9.01	0.17	9.32	0.14
	Sts	6.83	0.24	6.29	0.29
	Smp2a	2.44	0.94	2.4	1.26
	Ugt2b	1.43	0.87	1.71	0.99
Genistein	Cyp11a1	6.01	0.57	5.07	0.37
	Cyp17a1	1.07	0.32	1.71	1.09
	Hsd3b	3.22	1.06	3.53	0.94
	Hsd17b3	4.1	0.81	2.82	0.85
	Hrmt1l2	9.18	0.21	9.44	0.21
	Sts	6.47	0.38	6.25	0.21
	Smp2a	3.04	1.04	2.36	0.97
	Ugt2b	1.62	1.16	1.39	1.15
Resveratrol	Cyp11a1	6.43	0.34	5.45	0.4
	Cyp17a1	1.3	0.38	1.35	0.71
	Hsd3b	3	1.1	3.09	0.79
	Hsd17b3	3.3	1.09	3.58	0.66
	Hrmt1l2	9.15	0.19	9.44	0.21
	Sts	6.56	0.36	6.29	0.21
	Smp2a	2.5	0.93	2.06	1.01
	Ugt2b	1.86	0.96	1.51	0.76

is activated from day 21 to day 50. Specifically, two global tests (21-23) were employed to evaluate an overall gene expression change from day 21 to day 50 for each experimental group: a global test with random effects (22) and an ANOVA global test (23). The global test with random effects employs a generalized linear model with a random effect where the random effect is used

to examine the time effect from day 21 to day 50. The ANOVA global test is to test the association between gene expressions and the time factor by comparison of linear models through the extra sum of squares principle. Both approaches have been evaluated by Dinu *et al.* (24) and Fridley *et al.* (25) and show both have comparable power with similar P values and also have a higher

power than the Fisher test. Here we used 0.05 as the P value cut-off for the statistical significance level for both global tests. Univariate analysis for each individual gene was also performed by two-sample t-test to test any expression change from day 21 to day 50. The P value was adjusted for simultaneously multiple testing by the false discovery rate method (26). Then, a chain reaction model was used to simulate the estrogen synthesis pathway. In this model, the regulated genes are treated as a set of chemical species, and the gene change through a conversion process in the pathway is represented by the species change through a reaction channel of the chain reaction model. The chain reaction model involves a set of ordinary differential equations (ODEs) to represent the rates of species change. The reaction rates associated with each reaction channel are used to describe interactions between genes in the pathway. Since numerical errors may occur due to a stiffness problem (e.g., disparate changes of gene expression), we employ an implicit scheme to solve the set of ODEs. The implicit scheme is a numerical algorithm to linearize the gene expression change and approximate the reaction rates using the Taylor series expansion. Employment of the implicit scheme can increase numerical stability and accuracy.

Our hypothesis for this experiment is that the three polyphenols can affect gene expression in the estrogen synthesis pathway during puberty. Thus, we expect gene expression differences between the three treatment groups versus the control group. We first applied the chain reaction model to obtain reaction rates for the control group based on data at day 21 and day 50. A sensitivity study was conducted to evaluate how well the model fits to the control group data at day 50. In the sensitivity analysis, we added a certain degree of normal random noise (0.5 and 1 standard deviations) to expression data at day 21. The chain reaction model then analyzed these noise-added data to obtain a set of predicted expressions. These predicted expressions were compared to the predicted expressions that were estimated based on original data (i.e., no noise added). We computed the bias and mean square error (MSE) for evaluation. A smaller bias and MSE close to 0 indicates robustness of the model. Then the chain reaction model built based on the control group data was used to predict gene expression at day 50 for the three polyphenol groups. When these nutrients affect the estrogen synthesis pathway, we expect discrepancies between observed and expected gene expressions.

Results

Global test approaches to test overall gene expression on the estrogen synthesis pathway

Descriptive statistics and distribution of these 8 gene expressions are displayed in *Table 1* and *Figure 2*. Gene expression change from day 21 to day 50 yielded various patterns. For example in *Table 2A*, gene Cyp11a1 was down-regulated from day 21 to day 50 in the four experimental groups ($P=0.009-0.0001$). In contrast, gene Hrmt12 had similar expression between day 21 and day 50 in the control group, but was up-regulated from day 21 to day 50 in the other three polyphenol groups ($P=0.04-0.001$). Statistical data analysis based on the two global tests showed the overall expression changed significantly for the control ($P=0.044-0.048$) and genistein ($P=0.004-0.005$) groups based on the P value cutoff of 0.05, but not the EGCG ($P=0.27$) and resveratrol ($P=0.07$) groups (*Table 2B*). This observation indicates the estrogen synthesis pathway had been activated from pre- to post- puberty period based on the reference group (i.e., control group). As the nutrients intervened, the pathway was either less activated (e.g., EGCG and resveratrol) or moved to a higher significant activation level (e.g., genistein).

Chain reaction model to evaluate the estrogen synthesis pathway

In the present study, we propose an 8-channel chain reaction model, listed in *Table 3*, to simulate the estrogen synthesis pathway. The 8-channel chain reaction model is selected based on the UAB-CNGI's estrogen synthesis pathway shown in *Figure 1*. The reaction rates used in this chain reaction model, estimated based on the mean value of gene expression changes between day 21 and day 50 of the control group, are listed in *Table 3*. For example, gene Cyp11a regulates gene Cyp17 with a reaction rate, K_1 , in the model. Gene Hsd3b co-regulates with gene Cyp17 with a forward rate, K_2 , and a backward rate, K_3 . *Table 3* shows a negative reaction rate from Sts to Smp2a, and two zero rates from Hsd3b to Hsd17b3 and Ugt2b. The zero reaction rates indicate no appreciable gene expression change observed from the microarray data, while the negative reaction rate was caused by opposite trends between the microarray data and the estrogen synthesis pathway. The chain reaction model was employed to analyze the gene expression changes for the control group and 3 treatment groups (EGCG, genistein,

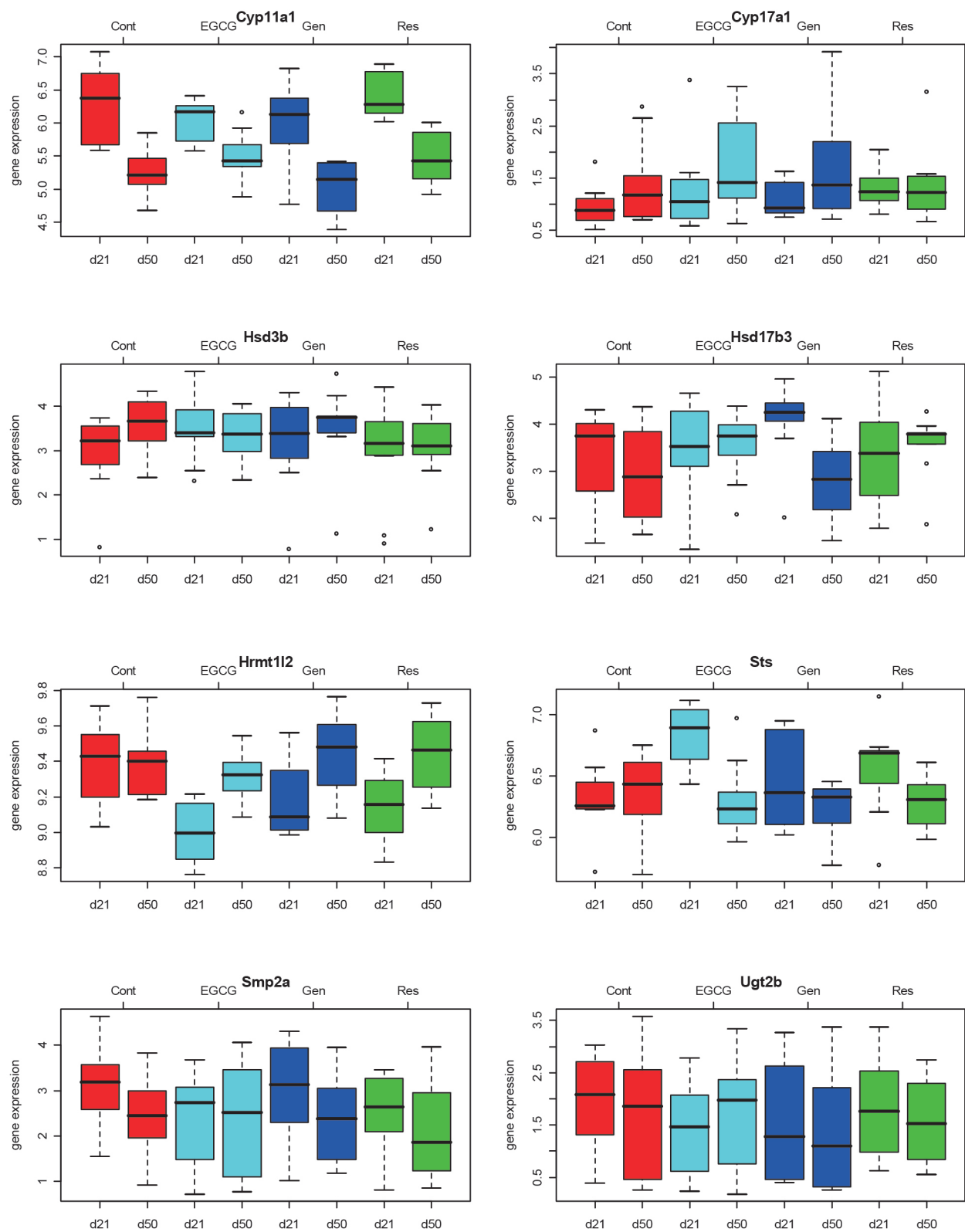


Figure 2 Distribution of gene expressions in estrogen synthesis pathway for the four treatment groups at day 21 and day 50

Table 2 Results of univariate analysis and global tests on estrogen synthesis pathway from day 21 to day 50

(A) Univariate analysis				
Adjusted P value [^]	Control	EGCG	Genistein	Resveratrol
Cyp11a1	0.009*	0.004*	0.004*	0.0001*
Cyp17a1	0.34	0.40	0.20	0.84
Hsd3b	0.34	0.78	0.57	0.84
Hsd17b3	0.81	0.78	0.01*	0.64
Hrmt1l2	0.95	0.001*	0.04*	0.02*
Sts	0.94	0.001*	0.20	0.13
Smp2a	0.34	0.94	0.20	0.59
Ugt2b	0.86	0.78	0.67	0.59
[^] P value was adjusted by FDR method. *P<0.05				
(B) Global tests				
P value	Global test with a random effect		ANOVA global test	
Control	0.044*		0.048*	
EGCG	0.27		0.27	
Genistein	0.004*		0.005*	
Resveratrol	0.07		0.07	
*P<0.05				

Table 3 Reaction rates of gene to gene in the estrogen synthesis pathway

Gene name	Reaction rate	Gene name
Cyp11a	K ₁ (0.152): →	Cyp17
Hsd3b	K ₂ (1.485): ←	Cyp17
	K ₃ (4.199): →	
Sts	K ₄ (0.519): →	Hsd3b
Sts	K ₅ (-0.215): →	Smp2a
Hsd3b	K ₆ (0): →	Hsd17b3
Hsd3b	K ₇ (0.089): →	Hrmt1/2
Hsd3b	K ₈ (0): →	Ugt2b

and resveratrol), and the predicted gene expressions at Day 50 are shown in *Table 4*. The difference between the numerical results and the observed data in the control group ranges from -0.18 to 0.22. In the sensitivity analysis, *Table 5* shows smaller biases and mean square errors (MSE) for 0.5 and 1 standard deviations (SD) (bias: -0.092~0.214 for 0.5 SD and -0.162~0.254 for 1 SD; MSE: 0.011~0.258 for 0.5 SD and 0.057~0.557 for 1 SD). The sensitivity analysis results indicate that the model is robust to a small amount of random noise (at least within 1 SD). The similarity in the range of difference between the control group in *Table 1* and that in the sensitivity analysis result for 1 SD (-0.18~0.22 versus -0.162~0.254) suggests that the model has a good fit for the control

group. Moreover, it is expected that there is a discrepancy between the numerical result and the observed results in the treatment groups at Day 50 due to the effect of nutrient diets. The results showed some genes with a large discrepancy between the predicted and observed values, such as Hsd3b and Sts in the EGCG group, and Hsd3b and Hrmt12 in the resveratrol group. These observations suggest nutrient effects in gene expression on this pathway, and, consequently, suggest that the chain reaction model can be estimated for different treatments. Further study can be conducted to obtain the reaction rates for different diet treatment groups and to correlate the nutrient effect on the reaction rates of the estrogen synthesis pathway.

Discussion

In this paper, we have presented an animal experiment using the microarray technology to study nutrient-gene effects. Since the effects of polyphenols on the estrogen synthesis pathway are not fully understood, this experiment is valuable and allows us to examine how the nutrient-containing diets affect gene expression during puberty. The results may help scientists understand the effect of nutrients on genes and develop effective prevention approaches to reduce cancer risk. To evaluate an overall gene expression change from day 21 to day 50, we

Table 4 Prediction of gene expression at day 50

Experimental group	Day 50	Gene name							
		Cyp11a1	Cyp17a1	Hsd3b	Hsd17b3	Hrmt1l2	Sts	Smp2a	Ugt2b
Control	Observed	5.24	1.4	3.52	2.98	9.38	6.34	2.4	1.73
	Predicted	5.25	1.32	3.33	3.2	9.31	6.3	2.41	1.88
EGCG	Observed	5.48	1.76	3.35	3.6	9.32	6.29	2.4	1.71
	Predicted	5.26	1.56	4	3.42	9.36	6.92	2	1.42
Genistein	Observed	5.07	1.71	3.53	2.82	9.44	6.25	2.36	1.39
	Predicted	4.82	1.37	3.48	3.84	8.92	6.28	2.34	1.53
Resveratrol	Observed	5.45	1.35	3.09	3.58	9.44	6.29	2.06	1.51
	Predicted	5.37	1.41	3.6	3.18	9.08	6.42	1.93	1.77

Table 5 Sensitivity analysis for evaluation of prediction performance

Degrees of random noise		Gene name							
		Cyp11a1	Cyp17a1	Hsd3b	Hsd17b3	Hrmt1l2	Sts	Smp2a	Ugt2b
0.5 SD	Bias	0.007	-0.036	-0.092	0.214	0.033	0.02	-0.079	-0.066
	MSE	0.045	0.011	0.084	0.258	0.026	0.055	0.048	0.233
1 SD	Bias	0.254	-0.013	-0.069	-0.02	0.139	-0.033	-0.162	-0.096
	MSE	0.399	0.057	0.421	0.557	0.181	0.084	0.15	0.457

Note: 1. Random noise was generated using standard normal distribution with 0.5 and 1 standard deviations. We simulated data 100 times. 2. SD=standard deviation. 3. MSE=mean square error

employed two global tests to evaluate association of the estrogen synthesis pathway with the time effect (22,23). To study gene-gene interaction, we applied a chain reaction model to simulate the pathway. Although the chain reaction model has been widely used to simulate chemical reactions in the engineering field, this is the first application of this approach to microarray data to the best of our knowledge. The use of the chain reaction model to simulate gene expression changes is a novel application because we translated the gene pathway into a set of chemical reactions in which each reaction channel describes gene-gene interaction in the pathway. Moreover, to address the numerical error issue in the chain reaction model, the implicit scheme was employed to solve the differential equations. The implicit scheme linearizes the gene expression change and approximates the reaction rates with the Taylor series expansions such that numerical stability and accuracy can be increased.

However, due to the limitations of this microarray experiment, the reaction rates used in this study were estimated based on available data at two time slices. Hence, the gene expression change is dependent upon the reaction rates and a linear function of the gene

concentrations. This deficiency can be overcome in the future once the test data at various time slices are available to compute the reaction order for each reaction. This additional data will enable us to predict the non-linear gene expression changes throughout puberty, and not just at the end of the puberty cycle. Despite this deficiency, the result of applying the present model to the example data set with a control and 3 three polyphenol treatments provides assessment of the influence of different nutrient treatments on different genes. For example in *Table 4*, both EGCG and resveratrol groups showed some genes in which the predicted expression greatly differed from the observed value. This observation indicates both nutrients affect the estrogen synthesis pathway, especially for Hsd17b3 and Hrmt1l2 in the resveratrol group, and Hsd3b and Sts in the EGCG group when compared to the control group. The results are consistent with those of the global tests which yielded different statistically significant levels between the EGCG and the resveratrol groups versus the control group.

Lastly, we would like to point out that the present model is a deterministic approach; thus, it cannot account for the

dynamic effects, such as environmental exposure, dietary behavior change, and other unknown factors, which can also contribute to change in expression. Hence, a statistical sampling of the numerical result predicted by the present model is warranted in order to obtain the uncertainty and the margin of errors.

Methods

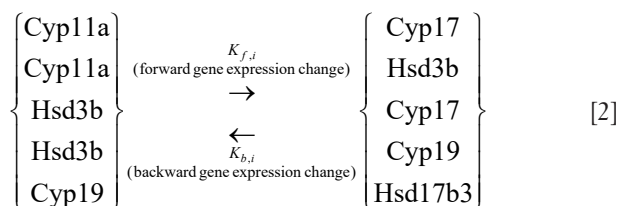
Chain reaction model

We propose a chain reaction model containing a set of chemical reactions to represent the pathway for the genes of interest, where each reaction channel represents a process of converting a gene to another one in the pathway. In this reaction model, we treat a set of regulated genes as a set of reacting species. By solving the species changes from the reaction model, the change of gene expression can be obtained.

The general form of the chain reaction model (27) can be expressed as

$$\sum_{j=1}^{ng} v'_{ij} \Phi_j \xleftrightarrow[K_{b,i}]{K_{f,i}} \sum_{j=1}^{ng} v''_{ij} \Phi_j \quad [1]$$

where v'_{ij} means stoichiometric coefficients of reactant gene j in reaction channel i , and v''_{ij} represents stoichiometric coefficients of product gene j in reaction channel i . $K_{f,i}$ and $K_{b,i}$ are forward and backward rates of gene expression changes in reaction channel i and were estimated based on the gene expression change from day 21 to day 50 (of the control group) obtained from the statistical analysis. Φ_j indicates the gene j , and ng means the number of genes involved in the chain reaction model. For example, the selected estrogen synthesis pathway contains several genes related to cholesterol, and part of the pathway can be expressed as



where Φ_j ($j=1, \dots, 5$) represent Cyp11a, Cyp17, Hsd3b, Cyp19, and Hsd17b3, respectively. In the present chain reaction model, the net expression change of gene j can be

calculated from the following equation:

$$\begin{aligned} \frac{dX_j}{dt} &= \sum_{i=1}^{nr} (v'_{ij} - v''_{ij}) K_{f,i} \prod_{k=1}^{ng} [X_k]^{r'_{ik}} + (v''_{ij} - v'_{ij}) K_{b,i} \prod_{k=1}^{ng} [X_k]^{r''_{ik}} \\ &= \sum_{i=1}^{nr} v_{ij} \left\{ K_{f,i} \prod_{k=1}^{ng} [X_k]^{r'_{ik}} - K_{b,i} \prod_{k=1}^{ng} [X_k]^{r''_{ik}} \right\} \end{aligned} \quad [3]$$

where nr is the number of reaction channels in the pathway model, and r'_{ik} (r''_{ik}) is the power dependence (or so-called reaction order) for reactant (product) gene k in reaction channel i . X_k is the concentration of gene k , defined as the ratio of the expression level of gene k to the sum of the expression levels of all the genes considered in this study. It can be seen that the gene expression change not only depends on the reaction rate, but also is a non-linear function of gene concentrations. This is the mathematical model commonly used in the kinetic chemistry for calculating the rate of concentration/fraction change. The use of multiplication is part of the mathematical model to account for the effect of the concentration of all participant genes as reactants. Since each reaction channel can contribute directly or indirectly to the expression change of a given gene, the total expression change rate of a given gene is the sum of the expression change rate associated with each reaction channel. In this preliminary study, the reaction order for all reaction channels is assumed to be unity in order to calculate the reaction rate since we only have data at two time slices (day 21 and day 50).

The chain reaction model involves a set of ordinary differential equations, and may pose a stiffness problem in obtaining a numerical solution (disparate changes of gene expression/species concentration at different time slices) (28-30). Typically, there are two numerical approaches to resolve the stiffness problem: an explicit scheme with a penalty function and an implicit scheme. These two numerical approaches are briefly described as follows.

Explicit scheme for solving the pathway equations

For the explicit scheme, gene concentrations can be calculated from the following equation.

$$X_j^{n+1} = X_j^n + \Delta X_j = X_j^n + \Delta t \left(\frac{dX_j}{dt} \right)^n = X_j^n + \Delta t f_j^n \quad [4]$$

where

$$f_j^n = \sum_{i=1}^{nr} v_{ij} \left\{ K_{f,i} \prod_{k=1}^{ng} [X_k^n]^{r'_{ik}} - K_{b,i} \prod_{k=1}^{ng} [X_k^n]^{r''_{ik}} \right\} \quad [5]$$

The superscripts, n and $n+1$, denote the values at the previous and current time steps, and Δt is the time-step size used for the time integration. The explicit scheme is a very simple method and is computationally efficient because the gene concentration at the next time level can be directly evaluated from the concentration at the previous time level (which is known). However, it may lead to large numerical errors if the reaction model is stiff. A penalty function can be employed to determine the appropriate time step size for integrating the gene expression change, such that the numerical error can be minimized. The penalty function can be expressed as

$$\frac{1}{\Delta t} = \max_j \left\{ \frac{f_j^n}{(\Delta X_j)_a} \right\} \quad [6]$$

where $(\Delta X_j)_a$ is a pre-set value of the maximum concentration change allowed. Though the penalty function can improve the numerical accuracy, the step size of time integration can be extremely small throughout the time domain, and thus the overall computational time (number of integration steps) can become very long. In addition, the numerical accuracy of this method is highly dependent upon the selected value of maximum concentration change allowed. Hence, users need some experience in order to determine an appropriate value for this parameter.

Implicit scheme for solving the pathway equations

For the implicit scheme, the gene concentrations are calculated based on

$$X_j^{n+1} = X_j^n + \Delta X_j = X_j^n + \Delta t \left(\frac{dX_j}{dt} \right)^{n+1} = X_j^n + \Delta t f_j^{n+1} \quad [7]$$

where

$$f_j^{n+1} = \sum_{i=1}^{nr} \nu_{ij} \left\{ K_{f,i} \prod_{k=1}^{ng} [X_k^{n+1}]^{r'_{ik}} - K_{b,i} \prod_{k=1}^{ng} [X_k^{n+1}]^{r''_{ik}} \right\} \quad [8]$$

It can be seen that unknowns (X_j^{n+1}, f_j^{n+1}) appear on both the right and left hand sides of the equations; hence, the set of equations cannot be solved directly. Taylor's series expansion was employed to linearize the production/dissipation rate term f_j^{n+1} , and can be expressed as

$$f_j^{n+1} = f_j^n + \sum_{k=1}^{ng} \left(\frac{\partial f_j}{\partial X_k} \right)^n (X_k^{n+1} - X_k^n) = f_j^n + \sum_{k=1}^{ng} \left(\frac{\partial f_j}{\partial X_k} \right)^n \Delta X_k^{n+1} \quad [9]$$

Using different approximations to achieve various orders of numerical accuracy, a general form of a set of algebraic equations can be obtained as

$$\Delta X_j^{n+1} - \sum_{k=1}^{ng} A_{j,k} \Delta X_k^{n+1} = C_3 f_j^n \quad \text{or} \quad BY = S \quad [10]$$

where

$$A_{j,k} = C_1 D_{j,k} + C_2 D_{j,k}^2 \quad \text{and} \quad D_{j,k} = \left(\frac{\partial f_j}{\partial X_k} \right)^n \quad [11]$$

$$B = \begin{bmatrix} 1-A_{1,1} & -A_{1,2} & \cdots & -A_{1,ng-1} & -A_{1,ng} \\ -A_{2,1} & 1-A_{2,2} & \cdots & -A_{2,ng-1} & -A_{2,ng} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ -A_{ng-1,1} & -A_{ng-1,2} & \cdots & 1-A_{ng-1,ng-1} & -A_{ng-1,ng} \\ -A_{ng,1} & -A_{ng,2} & \cdots & -A_{ng,ng-1} & 1-A_{ng,ng} \end{bmatrix} \quad [12]$$

$$Y = \begin{Bmatrix} \Delta X_1^{n+1} \\ \Delta X_2^{n+1} \\ \vdots \\ \Delta X_{ng-1}^{n+1} \\ \Delta X_{ng}^{n+1} \end{Bmatrix} ; \quad S = C_3 \begin{Bmatrix} f_1^n \\ f_2^n \\ \vdots \\ f_{ng-1}^n \\ f_{ng}^n \end{Bmatrix}$$

Table 6 Numerical order of implicit function

	1st-order implicit	2nd-order implicit	4th-order implicit
C_1	Δt	$\Delta t/2$	$\Delta t/2$
C_2	0	0	$-(\Delta t)^2/12$
C_3	Δt	Δt	Δt

The values of C_1 , C_2 , and C_3 for different orders of numerical accuracy are listed in Table 6, respectively.

Though the implicit methods require solving the matrix, the possible numerical error due the stiffness problem can be greatly reduced. In addition, users do not have to select an ad-hoc value for the allowable maximum gene changes. Therefore, we employed the implicit scheme to solve the chain reaction model of the pathway. The numerical accuracy of the employed implicit scheme has been demonstrated by solving a much stiffer chemical reaction such as hydrogen-oxygen and hydrocarbon-oxygen reactions, and the result was published previously (15,16).

Acknowledgments

We thank Mrs. Connie Pitts for secretarial assistance.

Funding: This work was supported by grants from the National Cancer Institute (5P30 CA-13148, 1P50 CA89019, and 1U54 CA100949).

Footnote

Conflicts of Interest: All authors have completed the ICMJE uniform disclosure form (available at <http://dx.doi.org/10.3978/j.issn.2218-676X.2012.05.06>). DTC serves as an unpaid editorial board member of *Translational Cancer Research*. The other authors have no conflicts of interest to declare.

Ethical Statement: The authors are accountable for all aspects of the work in ensuring that questions related to the accuracy or integrity of any part of the work are appropriately investigated and resolved.

Open Access Statement: This is an Open Access article distributed in accordance with the Creative Commons Attribution-NonCommercial-NoDerivs 4.0 International License (CC BY-NC-ND 4.0), which permits the non-commercial replication and distribution of the article with the strict proviso that no changes or edits are made and the original work is properly cited (including links to both the formal publication through the relevant DOI and the license). See: <https://creativecommons.org/licenses/by-nc-nd/4.0/>.

References

1. Available online: <http://www.heflingenetics.uab.edu/cngi/esp/pathway.html>
2. Henning SM, Niu Y, Lee NH, et al. Bioavailability and antioxidant activity of tea flavanols after consumption of green tea, black tea, or a green tea extract supplement. *Am J Clin Nutr* 2004;80:1558-64.
3. Davis CD, Milner J. Frontiers in nutrigenomics, proteomics, metabolomics and cancer prevention. *Mutat Res* 2004;551:51-64.
4. Go VL, Nguyen CT, Harris DM, et al. Nutrient-gene interaction: metabolic genotype-phenotype relationship. *J Nutr* 2005;135:3016S-20S.
5. Surh YJ. Cancer chemoprevention with dietary phytochemicals. *Nat Rev Cancer* 2003;3:768-80.
6. Arts IC, Hollman PC. Polyphenols and disease risk in epidemiologic studies. *Am J Clin Nutr* 2005;81:317S-25S.
7. Dahlquist KD, Salomonis N, Vranizan K, et al. GenMAPP, a new tool for viewing and analyzing microarray data on biological pathways. *Nat Genet* 2002;31:19-20.
8. Joshi-Tope G, Gillespie M, Vastrik I, et al. Reactome: a knowledgebase of biological pathways. *Nucleic Acids Res* 2005;33(Database issue):D428-32.
9. Kanehisa M, Goto S, Hattori M, et al. From genomics to chemical genomics: new developments in KEGG. *Nucleic Acids Res* 2006;34(Database issue):D354-7.
10. Kanehisa M, Goto S, Kawashima S, et al. The KEGG resource for deciphering the genome. *Nucleic Acids Res* 2004;32(Database issue):D277-80.
11. Shannon P, Markiel A, Ozier O, et al. Cytoscape: a software environment for integrated models of biomolecular interaction networks. *Genome Res* 2003;13:2498-504.
12. Available online: <http://www.biocarta.com>
13. Doniger SW, Salomonis N, Dahlquist KD, et al. MAPPFinder: using Gene Ontology and GenMAPP to create a global gene-expression profile from microarray data. *Genome Biol* 2003;4:R7.
14. Pandey R, Guru RK, Mount DW. Pathway Miner: extracting gene association networks from molecular pathways for predicting the biological significance of gene expression microarray data. *Bioinformatics* 2004;20:2156-8.
15. Cheng GC, Anderson P, Farmer RC. Development of CFD model for simulating gas/liquid injectors in rocket engine. In. 33rd AIAA/ASME/SAE/ASEE Joint Propulsion Conference 1997:97-3228.
16. Cheng GC, Farmer RC, Chen YS. Numerical study of turbulent flows with compressibility effect and chemical reactions. In. 6th AIAA/ASME Joint Thermophysics and Heat Transfer Conference 1994:94-2026.
17. Flynn KM, Ferguson SA, Delclos KB, et al. Effects of genistein exposure on sexually dimorphic behaviors in rats. *Toxicological sciences: an official journal of the Society of Toxicology* 2000;55:311-9.
18. Wang ZY, Khan WA, Bickers DR, et al. Protection against polycyclic aromatic hydrocarbon-induced skin tumor initiation in mice by green tea polyphenols. *Carcinogenesis* 1989;10:411-5.
19. Mentor-Marcel R, Lamartiniere CA, Eltoum IE, et al. Genistein in the diet reduces the incidence of poorly differentiated prostatic adenocarcinoma in transgenic mice (TRAMP). *Cancer Res* 2001;61:6777-82.
20. Chen DT. A graphical approach for quality control of oligonucleotide array data. *J Biopharm Stat* 2004;14:591-606.
21. Goeman JJ, Oosting J, Cleton-Jansen AM, et al. Testing

- association of a pathway with survival using gene expression data. *Bioinformatics* 2005;21:1950-7.
22. Goeman JJ, van de Geer SA, de Kort F, et al. A global test for groups of genes: testing association with a clinical outcome. *Bioinformatics* 2004;20:93-9.
 23. Hummel M, Meister R, Mansmann U. GlobalANCOVA: exploration and assessment of gene group effects. *Bioinformatics* 2008;24:78-85.
 24. Dinu I, Potter JD, Mueller T, et al. Gene-set analysis and reduction. *Brief Bioinform* 2009;10:24-34.
 25. Fridley BL, Jenkins GD, Biernacka JM. Self-contained gene-set analysis of expression data: an evaluation of existing and novel methods. *PLoS ONE* 2010;5:pii: e12693.
 26. Benjamini Y, Hochberg Y. Controlling the false discovery rate: a practical and powerful approach to multiple testing. *J R Stat Soc B* 1995;57:289-300.
 27. Farmer RC, Cheng GC, Chen Y-S, et al. Computational Transport Phenomena for Engineering Analyses. In: CRC Press, Taylor & Francis Group; 2009.
 28. Curtis CF, Hirschfelder J. Integration of stiff equations. *Proc Natl Acad Sci USA* 1952;38:235.
 29. DeGroat J, Abbett M. A computation of one-dimensional combustion of methane. *AIAA J* 1965;3:381-3.
 30. Moretti G. A new technique for the numerical analysis of nonequilibrium flows. *AIAA J* 1965;3:223-9.

Cite this article as: Cheng GC, Chen DT, Chen JJ, Soong SJ, Lamartiniere CA, Barnes S. A chain reaction approach to modelling gene pathways. *Transl Cancer Res* 2012;1(2):61-73. DOI: 10.3978/j.issn.2218-676X.2012.05.06